



Polytechnic Tutoring Center

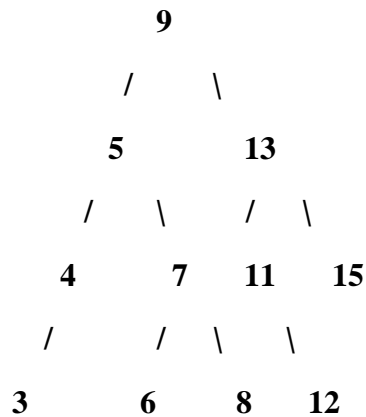
Final Exam Review ANSWER KEY

CS 1134, Fall 2021

Disclaimer: This mock exam is only for practice. It was made by tutors in the Polytechnic Tutoring Center and is not representative of the actual exam given by the CS Department.

1. Given the preorder traversal of a binary search tree is as follows: 9 5 4 3 7 6 8 13 11 12 15...

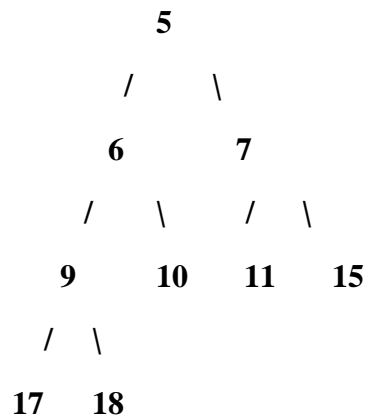
a. Draw the described tree.



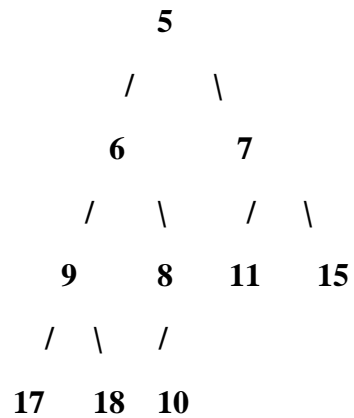
b. Now that you have the tree, what is its postorder traversal?

3 4 6 8 7 5 12 11 15 13 9

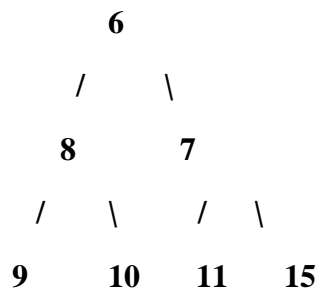
2. Given a min heap with the structure as defined below, redraw the minheap after performing the following operations...



- a. Insert 8



- b. Delete min



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17 18

3. Write a function which recursively determines if a binary tree is balanced or not. By balanced, we mean that the right and left subtrees have at most a difference in height of 1. Note: You may use a helper if this helps you.

```
def is_height_balanced(root):  
    def balanced_helper(root):  
        if not(root.left) and not(root.right):  
            return (1, True)  
        elif not(root.right):  
            right = balanced(root.right)  
            if right[0] > 1:  
                return (right[0] + 1, False)  
            else:  
                bal = right[1]  
                return (right[0] + 1, bal)  
        elif not(root.left):  
            left = balanced(root.left)  
            if left[0] > 1:  
                return (left[0], False)  
            else:  
                bal = left[1]  
                return (left[0] + 1, bal)  
        else:
```

```

right = balanced(root.right)
left = balanced(root.left)
bal = right[1] and left[1]
height_condition = abs(right[0] - left[0]) <= 1
return (max(right[0], left[0])+1, bal and height_condition)

```

```

if not(root):

```

```

    raise Exception("Empty Tree")

```

```

else:

```

```

    return balanced_helper(root)[1]

```

4. Define a non-recursive function which will print out the specified level of a tree, using only a stack and a queue and constant additional space.

```

def print_tree_level(root, level):

```

```

    q = ArrayQueue()

```

```

    s = ArrayStack()

```

```

    q.enqueue(root)

```

```

    count = 1

```

```

    while not(q.is_empty()) and count < level:

```

```

        curr = q.dequeue()

```

```

        if curr.left:

```

```

            s.push(curr.left)

```

```

        if curr.right:

```

```

            s.push(curr.right)

```

```

        if q.is_empty():

```

```

            count += 1

```

```

            while not(s.is_empty()):

```

```

                q.enqueue(s.pop())

```

```

    if q.is_empty():

```

```

        return

```

```

    else:

```

```

        while not(q.is_empty):

```

```

            print(q.dequeue().data)

```

5. Draw the resultant Hash Table after inserting the below items into the table (of size 13), with hash function $h(k) = k \bmod 13$. Use linear probing to deal with the collisions.

Insert 32, 5, 23, 29, 26, 41, 39, 42, 17, 19

26, 29, 41, 29, 42, 5, 32, 17, 19, __, 23, __, ____