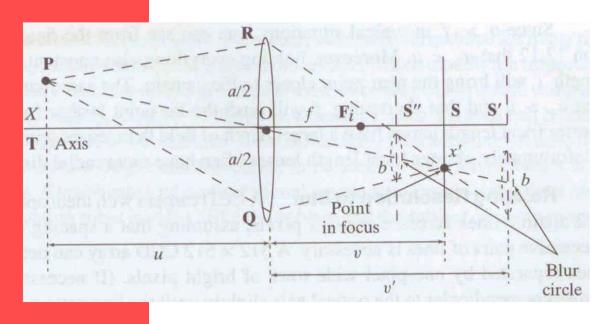


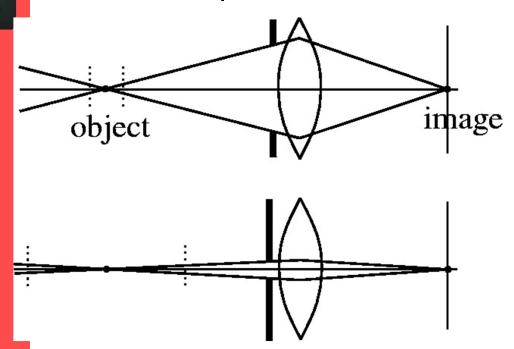
planes where blur is tolerable



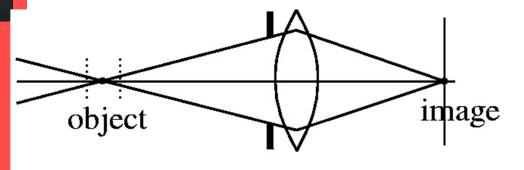
Thin lens: scene points at distinct depths come in focus at different image planes.

(Real camera lens systems have greater depth of field.)

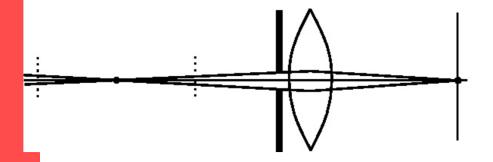
w does the aperture affect the depth of field?



w does the aperture affect the depth of field?



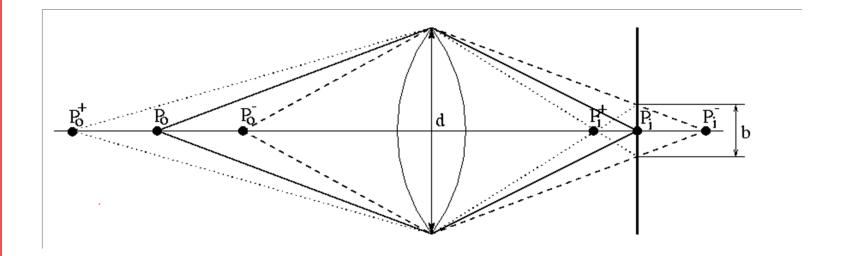




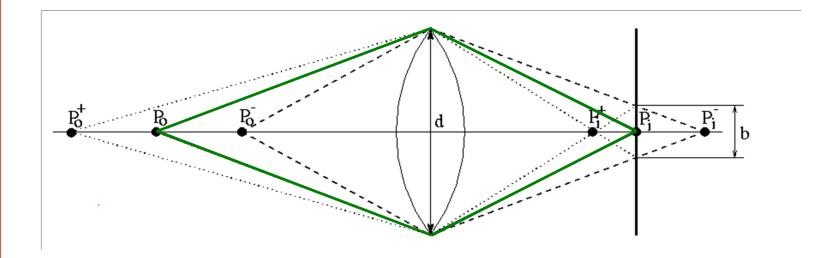


• A smaller aperture increases the range in which the object is approximately in focus

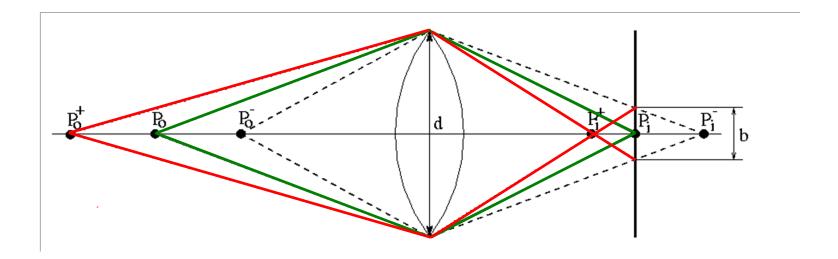






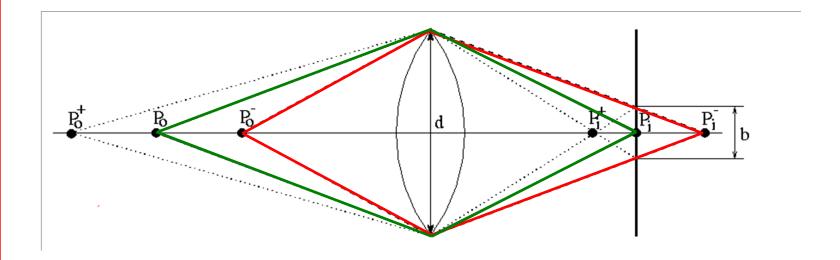






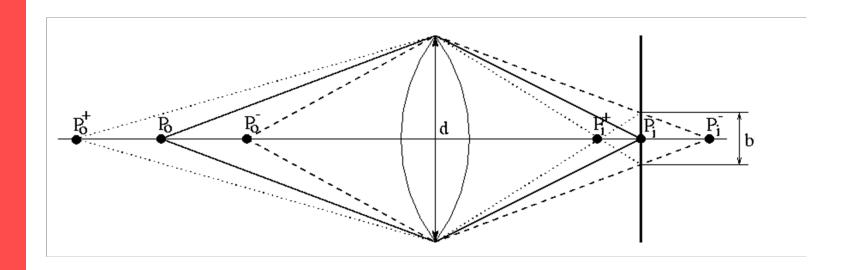








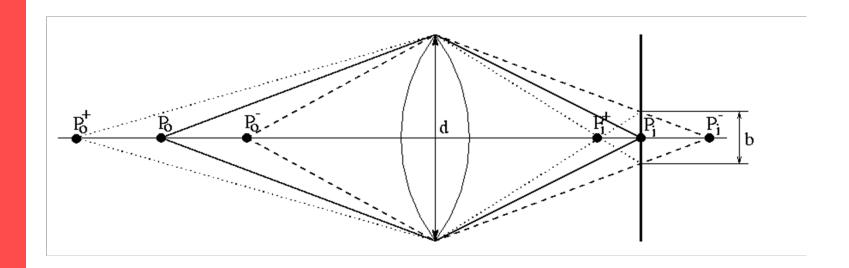
$$\frac{1}{Z_o^-} + \frac{1}{\left|Z_i^-\right|} = \frac{1}{f}$$







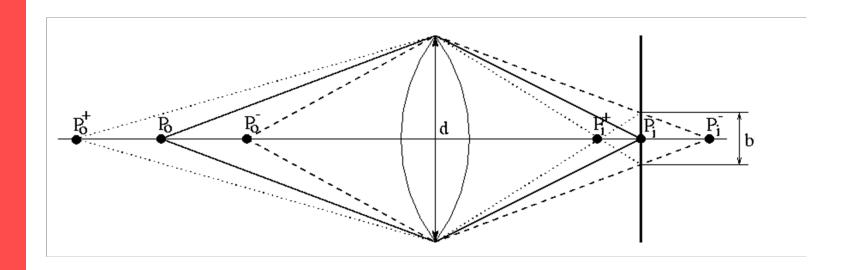
yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$





yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$

$$\left|Z_{i}^{-}\right| = \left|Z_{i}\right| + \Delta Z_{i}^{-}$$

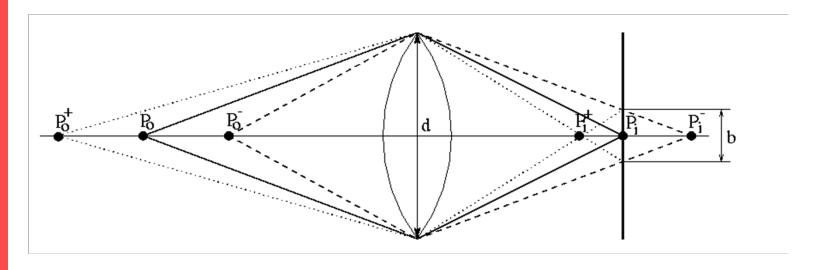




yields
$$Z_{o}^{-} = f \frac{\left|Z_{i}^{-}\right|}{\left|Z_{i}^{-}\right| - f}$$

$$\left| Z_i^- \right| = \left| Z_i \right| + \Delta Z_i^-$$

$$\frac{\Delta Z_i^-}{b} = \frac{\left|Z_i\right| + \Delta Z_i^-}{d}$$

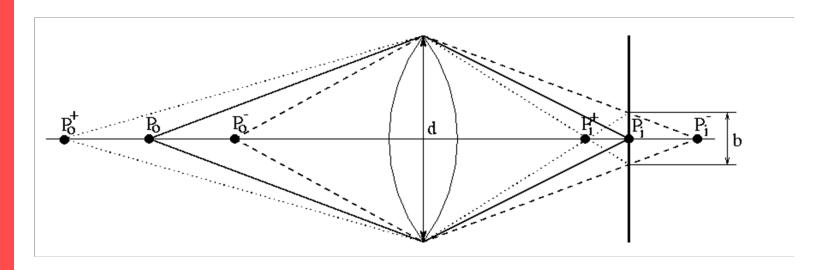




yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$

$$\left| Z_i^- \right| = \left| Z_i \right| + \Delta Z_i^-$$

$$\Delta Z_i^- = \frac{b}{d-b} |Z_i|$$

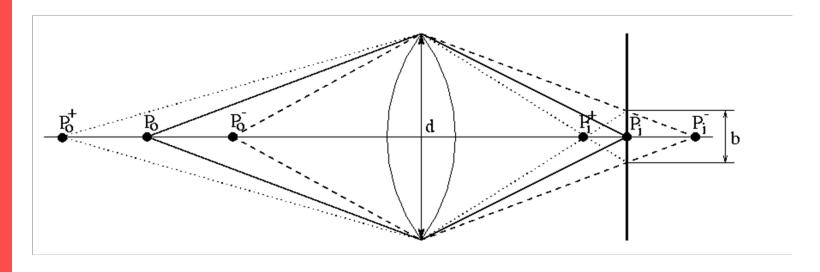




yields
$$Z_{o}^{-} = f \frac{\left|Z_{i}^{-}\right|}{\left|Z_{i}^{-}\right| - f}$$

$$\left|Z_{i}^{-}\right| = \left|Z_{i}\right| + \Delta Z_{i}^{-}$$

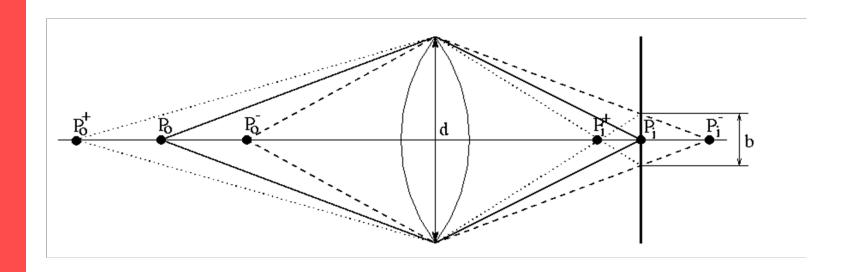
$$\sum_{i=1}^{m} \frac{b}{d-b} |Z_i|$$





yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$

$$\left| \left| Z_i^{-} \right| = \left| Z_i \right| d / (d - b)$$





yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f} \left| \left| Z_i \right| = \frac{f Z_o}{Z_o - f} \right|$$

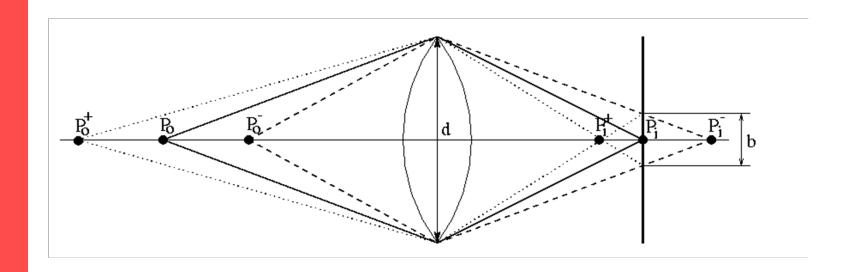
$$P_0^+$$
 $P_0^ P_1^ P_1^$





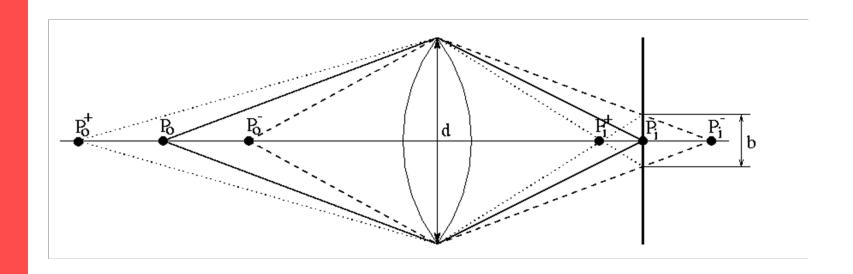
yields
$$Z_o^- = f \frac{\left|Z_i^-\right|}{\left|Z_i^-\right| - f}$$

$$\frac{\left|Z_i^-\right|}{\left|Z_i^-\right| - f} = \left|Z_i\right| d/(d-b)$$





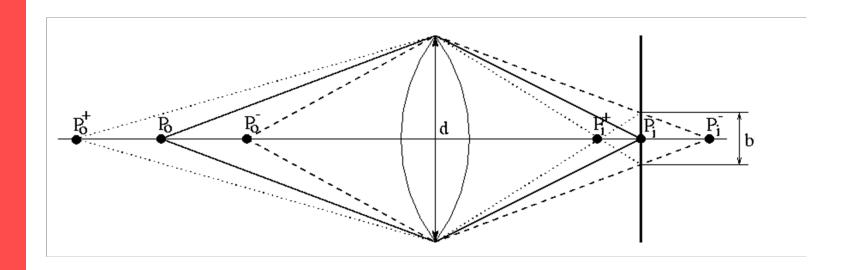
yields
$$Z_o^- = f \frac{\left|Z_i^-\right|}{\left|Z_i^-\right| - f} = \frac{f Z_o}{Z_o - f}$$





yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$

$$Z_o^- = f \frac{d Z_o}{b Z_0 + f (d - b)}$$





yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$

$$Z_{o}^{-} = f \frac{d Z_{o}}{b Z_{0} + f (d - b)}$$

$$\Delta Z_{o}^{-} = Z_{o} - Z_{o}^{-} = \frac{Z_{o} (Z_{o} - f)}{Z_{0} + f d / b - f}$$





yields
$$Z_o^- = f \frac{\left| Z_i^- \right|}{\left| Z_i^- \right| - f}$$

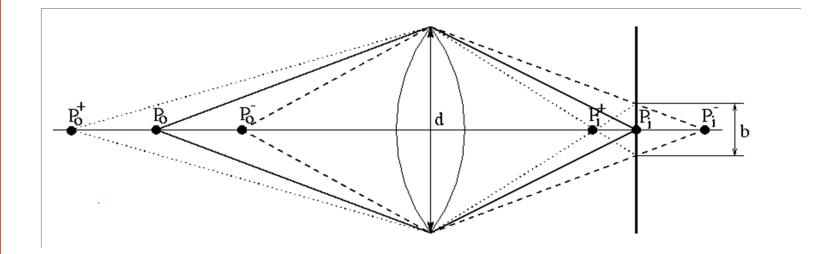
$$Z_{o}^{-} = f \frac{d Z_{o}}{b Z_{0} + f (d - b)}$$

$$\Delta Z_{o}^{-} = Z_{o} - Z_{o}^{-} = \frac{Z_{o} (Z_{o} - f)}{Z_{0} + f d/b - f}$$

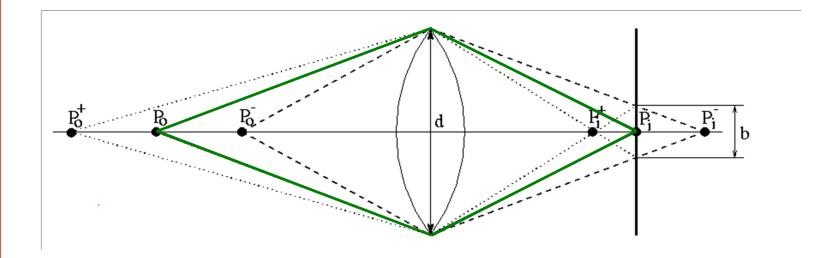
Similar formula for
$$\Delta Z_o^+ = Z_o^+ - Z_o$$



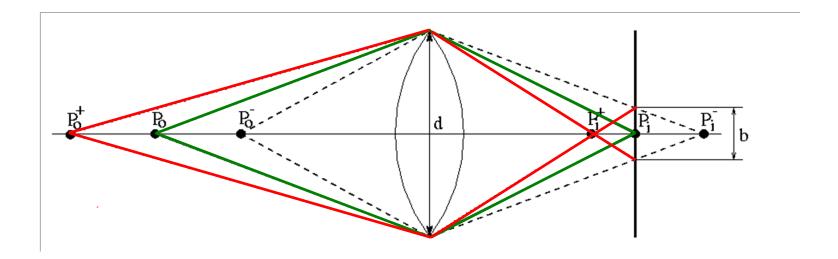






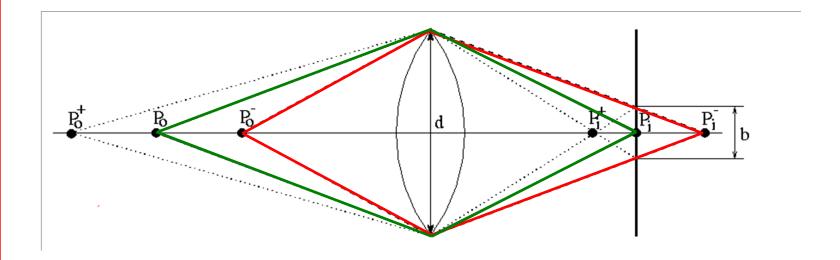




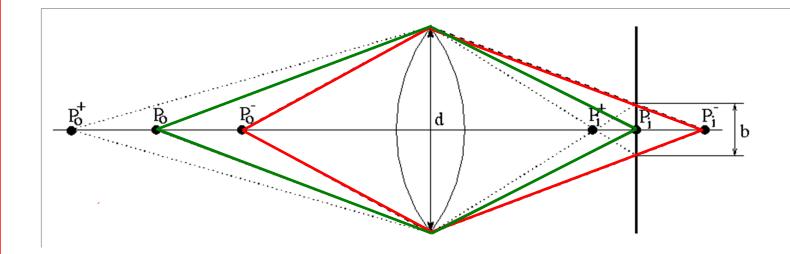








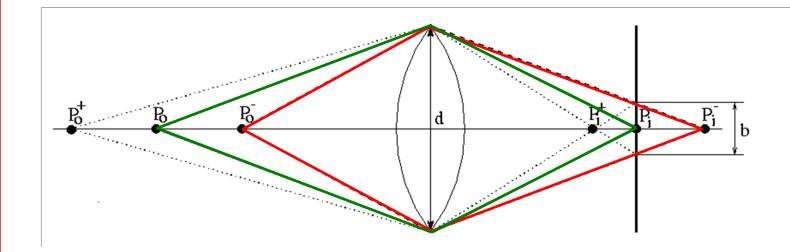




$$\Delta Z_0^- = Z_0 - Z_0^- = \frac{Z_0(Z_0 - f)}{Z_0 + f d/b - f}$$





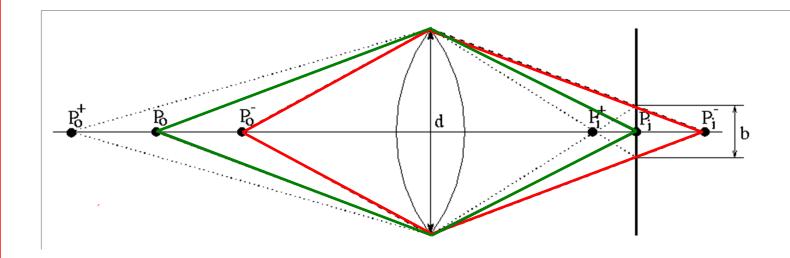


$$\Delta Z_0^- = Z_0 - Z_0^- = \frac{Z_0(Z_0 - f)}{Z_0 + f d/b - f}$$

decreases with d+, increases with Z_0 +







$$\Delta Z_0^- = Z_0 - Z_0^- = \frac{Z_0(Z_0 - f)}{Z_0 + f d/b - f}$$

decreases with d+, increases with Z₀+ strike a balance between incoming light and sharp depth range

